# QUALITY ANALYSIS OF 3D ROAD RECONSTRUCTION

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#### ABSTRACT:

Quality of 3D reconstructed roads strongly depends on input data and following processing steps. Quality analysis is essential for building up a reliable reconstruction process and for a proper use of 3D data. It is therefore of interest to analyse which error sources influence the final result, and what is the sensitivity of each of these error sources. In this paper we explicitly describe quality of 3D reconstructed roads as a function of input data. These 3D roads have been reconstructed automatically by a fusion process of two input data sets: topographic map data and airborne laser data. Heights of map points are calculated by least squares plane fitting through a selection of neighbouring laser points. We determine the precision of map point heights by using error propagation techniques and properties of least squares adjustment. Map points heights have been calculated with a precision varying from a few centimetres to a few decimetres, depending on the point density and distribution of laser data. Even more important is that independent reference data showed the correctness of predicted quality by testing the actual quality against the predicted quality.

### 1. INTRODUCTION

Reconstructing 3D topographic objects has been an active research topic in the last decade, driven by the growing need for 3D geo-information and the growing technical possibilities. Researchers proposed several acquisition techniques varying in terms of level of automation, focus on specific objects, and kinds of data sources like stereo imagery or laser altimetry data. Quality parameters of these 3D reconstructed models strongly depend on input data and how well these objects can be extracted from the data. (Kaartinen et al, 2005) reviewed the quality of building models submitted by 11 participants, and relate this to the acquisition methods, divided into image based and laser altimetry based approaches. In other individual papers sections on quality assessment are often limited to a value of success rate and completeness or a table of differences between reference data and reconstructed models.

While users of 3D geo-information also gained experiences in their applications, requirements on data quality became more specific. For one purpose users need a higher accuracy than for others. Quality descriptions are therefore essential for a proper use of data. For users as well as for researchers it is of interest to analyse which error sources influence the final result, and what is the sensitivity of each of these error sources.

In this paper we explicitly describe quality as a function of input data, using error propagation techniques and properties of least squares adjustment. Our focus is on the quality of 3D road reconstructions. We will examine the precision of only the height component in these models. Three-dimensional roads are important features for infrastructural analysis, like traffic noise simulations, but are also essential features in 3D city models, besides 3D buildings. Roads can automatically be reconstructed in 3D using airborne laser scanner data in combination with existing 2D map data (Oude Elberink and Vosselman, 2006). Their method recognises and models height discontinuities to allow roads to cross in 3D. Results have been shown for a

complex interchange, but quality assessment was limited to a section about completeness of the reconstructed model. First we will generally describe the reconstruction approach, which is an extension to the method of (Oude Elberink and Vosselman, 2006). By using formulas from least squares adjustments and error propagation techniques, we are able to analyse the precision and reliability of our reconstructed model. Finally, we check our reconstructed model by comparing it with independent reference data. Differences between these two datasets should be explainable by the predicted quality measures. Detailed insight in the quality of 3D reconstructed roads is important to analyse critical steps in the reconstruction process. This is especially true in situations in which laser points are scarce like on lower parts at interchanges. This paper gives insight in the quality of the 3D road reconstruction process and results.

#### 2. 3D ROAD RECONSTRUCTION

Essential in our quality analysis is the integration of functional and stochastic information, using error propagation and least squares adjustment techniques. In this section we describe the functional information, covering the subsequent steps to reconstruct 3D roads. Our aim is to reconstruct 3D road models by adding height values from laser data to 2D planar coordinates of map polygons.

## 2.1 Pre-processing

In a pre-processing stage laser data has been segmented into piecewise smooth laser segments. We have filtered small segments to remove points on objects like cars and traffic signs.

# 2.2 Assigning laser data to map data

Roughly, our approach assigns laser points to a map polygon and then reconstructs its 3D boundaries by fitting a plane through a selection of the assigned laser points. When reconstructing complex interchanges, assigning laser points to the map needs extra attention. Simple points-in-polygon operations will fail because the existence of roads on multiple height levels. Laser points should be assigned to a road part on the correct height level. In **Error! Reference source not found.** a part of an interchange is shown, visualizing map polygons bounded by black lines, and laser points coloured by height. Colours indicate height above mean sea level varying from yellow (~0 meter), green (~6 meter), blue (~14 meter) and purple (~21 meter).

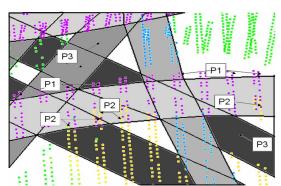


Figure 1. Laser points and map polygons at four height levels of a complex interchange, see text for explanations of P1, P2 and P3.

Looking at a complex infrastructural object like in Error! Reference source not found., the following characteristic problems may occur:

- P1. Due to a horizontal displacement between map and laser data, laser points will be assigned to the wrong (neighbouring) polygon.
- P2. Height data might be acquired at different levels at the same horizontal location because of the across track scanning angle. When reconstructing this map polygon at different height levels, we have to select the right laser points for the right height level, and remove the false laser points.
- P3. Problems arise when handling polygons with only a few points, due to the size of the polygon or due to the surface material of the object feature resulting in a low point density.

Problems mentioned above are solved in a special map growing algorithm. Map polygons are merged together if they belong to the same road. Geometric and topological information from two neighbouring polygons decides if they belong to the same road. Laser points are added during map merging if they fit to the height and slope of the growing map polygon. This assignment procedure is a recently added step to the approach of (Oude Elberink and Vosselman, 2006), making it possible to reconstruct complex interchanges completely and automatically, at all height levels. Now that laser points have been assigned to map polygons, the actual reconstruction consists of adding height values to each map point. To correctly capture the 3D shape of polygons, additional map points have been generated and inserted at every 10 meters. This height value is calculated by fitting a plane through a selection of laser points within a certain radius, see **Error! Reference source not found.**. This plane is calculated by least squares adjustment. To reduce influences of single laser points, only points from the largest segment have been used. The height of the plane at the location of the map point is taken as map point height. At road crossings multiple heights will be calculated and stored to make a full 3D description possible.

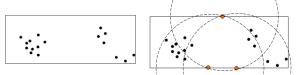


Figure 2. Laser points assigned to map polygon (left); map points (orange bullets) and search radius for selecting laser points (right).

Our plane parameters (p) can be written in the form:

$$z = f(x, y) = -xp_1 - yp_2 + p_3 \tag{1}$$

Where p1 and p2 are two slope parameters and p3 a distance parameter. We can write the plane calculation in a system of linear equations:

$$E\{y\} = Ax. \tag{2}$$

In equation (2), y contains observations (z-values of laser points), x is a vector of the three unknown plane parameters and matrix A contains information about the configuration of laser points. Each row consists of the horizontal location of a single laser point (-x, -y, 1).

$$E \begin{cases} z_1 \\ z_2 \\ z_3 \\ \dots \\ z_n \end{cases} = \begin{pmatrix} -x_1 & -y_1 & 1 \\ -x_2 & -y_2 & 1 \\ -x_3 & -y_3 & 1 \\ \dots & \dots & \dots \\ -x_n & -y_n & 1 \end{pmatrix} \begin{pmatrix} p_1 \\ p_2 \\ p_3 \end{pmatrix}.$$

$$(3)$$

To solve these equations in a least squares adjustment, observations are given a weight, and plane parameters are estimated by:

$$\hat{x} = (A^* Q_v^{-1} A)^{-1} A^* Q_v^{-1} y; Q_{\hat{x}} = (A^* Q_v^{-1} A)^{-1}.$$
(4)

After map height calculation, 3D boundaries are triangulated to get a solid surface description of the road. In the next section a quality description is given concerning the height values of 3D roads.

# 3. QUALITY DESCRIPTION

By using formulas from network design analysis, we can predict the quality of our reconstructed model before the actual reconstruction. For researchers quality prediction is useful for optimizing parameters used in their algorithms ("designing the network"). For users, predicting quality is important because it answers the question whether the input data and the processing steps can fulfil the user requirements.

We distinguish three components in the precision of the map point:

$$\sigma_{map\_pnt}^2 = \sigma_{plane}^2 + \sigma_{laser\_block}^2 + \sigma_{plane\_mdl}^2$$
(5)

 $\sigma_{plane}^2$  is the uncertainty caused by variations in the plane parameters, which are influenced by laser point noise.  $\sigma_{laser\_block}^2$  represents a stochastic value for systematic errors in laser data, and  $\sigma_{plane\_mdl}^2$  stands for discrepancies between the fitted plane and the actual shape of the road.

### 3.1 Quality of plane at map point location

To predict uncertainty in the plane parameters we need information about the quality and configuration of the input data. (Crombaghs et al., 2002) present a practical method to describe quality of laser data sets as a function of four error sources (error 1 to 4, denoted as E1 to E4). These error sources are point noise (E1), GPS (E2) and INS noise (E3) and strip adjustment noise (E4). Influence of each of these error sources depend on the size of the area of interest. Within the radius for selecting laser data, it can be expected that all laser points are influenced by the same E2, E3 and E4. When using least squares adjustment, these three error sources act as systematic errors, not stochastically influencing the quality of the plane equation. These error sources will be added later to the precision of the map point (see eq. 9). When only assuming influence of point noise in equation (4), Q<sub>y</sub> turns into a diagonal matrix and (4) can then be written in the form:

$$\hat{x} = (A^*A)^{-1}A^*y. {(6)}$$

Equation (6) shows that a diagonal matrix  $Q_y$  does not have an effect on the estimation of plane parameters. However, it does affect the quality of the plane parameters.

$$Q_{\hat{x}} = (A^* Q_y^{-1} A)^{-1} = \begin{pmatrix} \frac{1}{\sigma_z^2} & \sum_{i=1}^n x_i y_i & \sum_{i=1}^n - x_i \\ \sum_{i=1}^n x_i y_i & \sum_{i=1}^n y_i^2 & \sum_{i=1}^n - y_i \\ \sum_{i=1}^n - x_i & \sum_{i=1}^n - y_i & n \end{pmatrix}^{-1}$$

$$(7)$$

For a stable calculation we proceeded with local coordinates by subtracting the mean location of the laser points. Once the quality of plane parameters is known, we can calculate the height precision of the plane at the location of the map point.

$$\sigma_{plane}^2 = x^2 \sigma_{p_1}^2 + y^2 \sigma_{p_2}^2 + \sigma_{p_3}^2.$$
 (8)

# 3.2 Quality of laser block

Remember that equation (5) consisted of multiple components: plane uncertainty, systematic errors in laser data and model uncertainty. Laser point noise was taken into account in the plane uncertainty; other errors in laser data (E2, E3, and E4 as mentioned in section **Error! Reference source not found.**) did not reflect the plane equations. However, they influence the precision of the map point height. We can group these errors by:

$$\sigma_{laser\_block}^2 = \sigma_{E_2}^2 + \sigma_{E_3}^2 + \sigma_{E_4}^2 \tag{9}$$

# 3.3 Quality of plane model

Plane model quality covers the discrepancy at the map point between the actual shape of the road and the modelled plane. If the horizontal distance between map point and laser points is small it can be expected that a plane through these laser points accurately represents the road height at the map point. Model uncertainty becomes of interest when we need to extrapolate over a certain distance, in case we are short of laser points. We can quantify the differences between a local plane and the actual shape, by analysing the curvature of roads. To estimate the idealisation precision, we have to use height differences between plane and reality instead of curvatures. For distances smaller than a few hundred meters, we can approximate the difference between the road and a plane by a quadratic term.



Figure 3. Extrapolation error caused by model uncertainty.

**Error! Reference source not found.** can be translated into a stochastic measure for model uncertainty by calculating the standard deviation of extrapolation errors as a function of the distance. We have approximated this value by dividing maximum extrapolation error, calculated by integrating curvatures, by three.

#### 4. TESTING WITH REFERENCE DATA

In the previous sections we have described our 3D road reconstruction method and its stochastic model. To be able to test our *-functional* and *stochastic-* model, heights on reconstructed roads have been compared with independent reference data.

### 4.1 Reference data

Accurate geometric information of highways in the Netherlands is stored in a photogrammetrically derived topographic database, called DTB. Terrestrial measurements have been added to complete road information underneath interchanges and in tunnels. The DTB contains 3D geometric and semantic information of points, boundaries, centrelines and surface features of national roads, at a map scale of 1:1000. This also includes information on road details like locations of paint strips, traffic lights, road signs and other detailed infrastructural objects. DTM information (2.5D) has been integrated into the DTB by photogrammetric measurements on breaklines in the terrain. An example of DTB data is given, showing a complex interchange Prins Clausplein near The Hague.

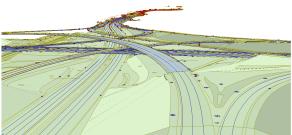


Figure 4. DTB data is used for reference information. Paint strips, shown as blue lines, have been selected to test reconstructed roads.

Paint strips have been measured by manual photogrammetric or tachymetric measurements. Paint strips belong to the so-called 'hard topography' category, what means that this object can be identified and measured with high precision. The standard deviation of heights of these points is required to be 9 cm or better.

## 4.2 Quality of 3D roads by comparing to reference data

In this section we will describe our testing configuration by comparing reference data with our reconstructed model. As we have seen in section **Error! Reference source not found.** roads are represented as a TIN surface, using 3D map points on the boundary as TIN nodes. **Error! Reference source not found.** explains the set-up of our height testing procedure. Orange bullets represent three map points that form one TIN triangle. Green plus marks represent 3D positions on paint strips, which are measured with high accuracy in the reference dataset. At these green plus marks height differences have been calculated.

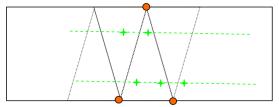


Figure 5. Configuration of height testing: TIN patches and points on paint strips.

Our expectation is that the height difference between reference data and our 3D model should vary around zero. Deviations should be explainable by uncertainty in the 3D model and in the reference data.

$$\Delta h_i = h_{\text{mod}_i} - h_{ref_i} \sim N(0, \sigma_{\Delta h_i})$$

$$\sigma_{\Delta h_i}^2 = \sigma_{h_{\text{mod}_i}}^2 + \sigma_{h_{ref_i}}^2$$
(10)

The term  $\sigma_{h_{\text{mod}_i}}^2$  contains the height variance of the model, at the location of the reference point. We therefore have to propagate precisions of the map points, calculated as described in section **Error! Reference source not found.**, to the location of the reference point. Looking again at **Error! Reference source not found.**, we see that the precision of three map points influence the precision at reference point location.

First, the location of the reference point within the TIN mesh is important to describe the influence each of the map points. If the reference point is close to one of the three map points, the precision of the TIN height is highly influenced by the precision of the height of this single map point. Then we investigate the influence of covariance between the three map points. Extreme cases here are no covariance and full covariance. If the three map point heights have been calculated by three different groups of laser points, we can assume that the correlation equals zero. This occurs when using a small radius to select laser points. If the three map point heights have been calculated by the same group of laser points, the correlation equals one.

# 4.3 Testing our predicted quality

In section Error! Reference source not found. we have calculated the precision of map point heights by using error propagation techniques and properties of least squares plane fitting, in this section followed by an actual quality check using reference data. To test the stochastic model we check if the actual differences can be explained by the predicted accuracy. With the outcomes of equation (10), we test if the difference is significant by using a modified version of the w-test statistics or local error detection as described by (Baarda, 1968 and Teunissen, 1991). In their approaches, the w-test calculates normalized residuals of geodetic observations. If the test exceeds a critical value, this observation will be recognized as a possible outlier. In an iterative procedure the observation with the highest w-test value has been removed from the adjustment.

$$w_i = \frac{\Delta h_i}{\sigma_{\Delta h_i}} \sim N(0,1) \tag{11}$$

A closer look at the  $w_i$  learns that it indicates how well one can predict the actual quality. This is an informative measure to show if the predicted quality represent the actual quality. If the stochastic model is correct, the total of all w-test values should have a standard normal distribution. To rely on predicted quality is important for future users who want to predict the quality of 3D reconstructed roads, without checking on highly detailed reference data. Besides this, reference data might not be available at some locations.

#### 5. RESULTS

### 5.1 Data specifications

For a complex interchange we assigned coarse laser data (~1 point/ 9m²) to a medium scale topographic map (1:10.000). Laser point noise has been determined in a quality control procedure at the Survey Department of Rijkswaterstaat. For this project the laser point noise (E1) has been stated to be 8 cm, GPS noise (E2) 3 cm, INS noise (E3) 4 cm and block uncertainty (E4) 3 cm. To estimate extrapolation errors due to model uncertainty, we analysed curvature of road heights.

## 5.2 Predicted standard deviation of map point heights

The lefthand side of Figure 6 shows predicted standard deviations of map point heights. The figure shows the position of map points, coloured by predicted standard deviation of the map point height. For visibility reasons the standard deviation has been classified into three categories: standard deviations larger than 50 cm (shown in red), larger than 20 cm (yellow), and below 20 cm (green). To better understand the cause of large variations at some locations, the blue box in shows the laser points used for 3D road reconstruction. The relation between lack of laser data and large height variations can easily be seen for locations in black ellipses. Point densities in these black ellipses drop to 1 point per 100 m<sup>2</sup>, with extremes to 1 point per 600 m<sup>2</sup>. At map point locations in those areas, map point heights show standard deviations of more than 50 cm. Two factors play an important role here. First, the plane has been determined by just a few laser points; standard deviations of laser points will have a great influence because they are not averaged out. Secondly, the search radius for finding enough laser points increases up to 50 or even 100 meter. This results in extrapolation errors rising up to 50 cm or more.

# 5.3 Comparison with reference data

Results of calculated differences at paint strip locations can be seen in Figure 6 (right), where differences are coloured as red (larger than 50 cm), yellow (larger than 20 cm) and green (below 20 cm). Note that reference data is not completely covering the interchange. Some parts of flyovers have not been measured in the reference data, test results are therefore locally missing. Still we calculated over 10.000 height differences for this area of 1.2 x 1.2 km.

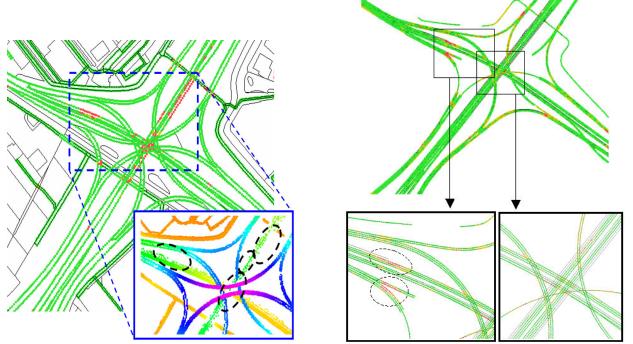


Figure 6. Standard deviations of map point heights (left). Height difference between reconstructed model and reference data (right).

A further look at Figure 6 learns that in the centre of the interchange (highlighted in the lower right corner box), where laser points were scarce at all height levels, the calculated differences are remarkably small. A few differences are more than 50 cm, some below 50 cm and many below 20 cm (green). In the lower left corner box, two situations are highlighted which show large height differences with a systematic character. In the higher circle height differences could be expected, due to the lack of laser points. The reason for differences in the lower circle is that the search radius selects laser points from both road parts, which happen to curve strongly at those locations. Therefore, fitting a plane through the selected points will differ from reality.

Table 1 summarizes most important statistic information of height differences between reference data and 3D reconstructed model. The mean difference includes systematic errors between reference data and our reconstructed model. Normally, it is expected to be in the order of 0-5 cm, due to systematic errors in laser data (Crombaghs et al., 2002). In this case, the mean difference happens to be very small (0.5 cm). Looking at the standard deviation of the differences of 15.4 cm, and knowing that it includes uncertainty in the reference data ( $\sigma_{ref} = 9$  cm), we can calculate the uncertainty of our reconstructed model ( $\sigma_{mod} = \operatorname{sqrt} (15.4^2 - 9^2) = 12.5$  cm). It should be noted that this value is biased by some systematic errors in the reconstructed model.

Number of reference points inside test area	10922
Mean difference	0.5 cm
Standard deviation of vector of differences	15.4 cm
Maximum absolute difference	121 cm

Table 1. Statistical results of comparing heights of 3D roads.

### 5.4 Testing predicted standard deviations

Now that the actual difference is known, we divide each difference with the expected standard deviation of the difference. In Figure 7 large w-test values have been coloured yellow (larger than 3) and red (larger than 4). At these points the actual height difference was three or four times larger than expected, meaning that either the standard deviation was too small or the calculated height was significantly wrong. Note that the former case deals with the stochastic model, and the latter case with the functional model. Due to the systematic character of large w-test values, we assume a functional error causes the problems at those locations, mostly where one road splits into two roads. However, the distribution of all w-tests is close to the standard normal distribution, as 68% of the w-test values are less than 1 and 92% are less than 2. If we remove outliers, standard deviation is 1.06 (with outliers 1.22). This means that the predicted stochastic model is a bit too optimistic, but still realistic.

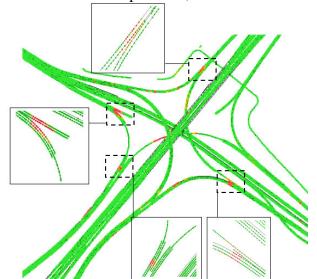


Figure 7. W-test values at reference point locations.

### 6. DISCUSSION

In this paper we have described a method to calculate quality of 3D reconstructed roads by error propagation. These 3D reconstructed models have automatically been acquired by a fusion process of map data and airborne laser data. After assigning laser data to map polygons, heights of map points have been calculated by least squares plane fitting through a selection of laser

points inside the polygon. These 3D map points are nodes in the 3D boundary description. Precision of the map point have been calculated by error propagation of laser point noise and the configuration of the laser points used for plane fitting. Influences of model uncertainty have been taken into account. Average predicted standard deviation of map point heights is about 10 cm.

Our method combines a 2D topographic data set with an airborne laser scanner dataset (2.5-3D). Even at locations where no height information is available, our method can reconstruct 3D roads with a height precision in the order of 10-15 cm. Input data sets used in this project are parts of national databases. Now that we can predict quality of 3D roads, we can predict the height quality for all roads in the national database without actually having to reconstruct them, and without testing them with reference data.

Independent reference data has been used to test our reconstructed model and its derived quality parameters. Predicted standard deviations realistically represent the actual quality for most of the situations. Exceptions are found at road splitting situations, where actual differences are more than four times higher than expected. The reason is the wrong assumption that a least squares fitted plane through the selected laser points, realistically represent the shape of the road. Future work will focus on improvement of reconstruction of these splitting roads. This can be achieved by selecting only those laser points that lie on the front side of the map point. The search algorithm for laser points should therefore not cross the polygon border.

Quality analysis as presented in this paper is not limited to 3D road reconstruction, but can be extended to other reconstruction applications. For example, building reconstruction can benefit from quality measures by error propagation. Decisions on conflictions between building knowledge and data driven information can be made more reliable if data driven approaches come with quality measures.

### **ACKNOWLEDGEMENT**

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