W eierstraß-Institut für Angewandte Analysis und Stochastik

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What is WIAS?
Why Delaunay grids? ...


## Outline

- Our interests in boundary conforming Delaunay grids.
- Your interests in Delaunay grids?
- The overlap?


The Delaunay grid and its dual: the Voronoi diagram.

## What's WIAS?

The Weierstrass Institute for Applied Analysis and Stochastics (WIAS) engages in project-oriented research in applied mathematics, particularly in applied analysis and applied stochastics, aiming at contributing to the solution of complex economic, scientific, and technological problems.


## What's WIAS?

Research Groups:

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## What's WIAS?

Main applications:

* nano- and optoelectronics,
* optimization and control of technical processes,
* phase transitions and multifunctional materials,
* stochastics in natural sciences and economics,
* flow and propagation processes in continua,
* numerical methods in analysis and stochastics.



## Van Roosbroeck's Equations

$$
\begin{align*}
& -\nabla \cdot \varepsilon \nabla \psi=f-n+p  \tag{1}\\
& \frac{\partial n}{\partial t}+\nabla \cdot \mu_{n} n \nabla \phi_{n}=R  \tag{2}\\
& \frac{\partial p}{\partial t}-\nabla \cdot \mu_{p} p \nabla \phi_{p}=R, \tag{3}
\end{align*}
$$

in $S \times \Omega, S=(0, T)$,
$\Omega \subset \mathbb{R}^{N}, 2 \leq N \leq 3$, a bounded Lipschitzian domain, $\partial \Omega=\Gamma_{D} \cup \Gamma, \Gamma_{D}$ closed, positive surface measure, $R=(n p-1) g(n, p), g(n, p)>0$ if $n, p>0$.
Boundary conditions ...
'Theorem': on any boundary conforming Delaunay grid the discrete problem (finite volume scheme) has at least one bounded steady state solution. The analytic and these discrete solutions fulfill identical bounds (depending on $f, R$, and boundary data).

## Summary



Thank you for the attention!


[^0]:    * Partial Differential Equations, Mielke
    * Laser Dynamics, Bandelow
    * Numerical Mathematics and Scientific Computing, Fuhrmann
    * Nonlinear Optimization and Inverse Problems, Hömberg
    * Interacting Random Systems, Bovier
    * Stochastic Algorithms and Nonparametric Statistics, Spokoiny
    * Thermodynamic Modeling and Analysis of Phase Transitions, Dreyer

