## **3D Data Structure Development**

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## History

- Adaptive surface data structures (TINs)
- Edge algebras (QEs)
- Dynamic map history management (Mioc)
- 2D Kinetic Voronoi (Anton, Yang, Mostafavi, Dakowicz)
- Importance of the dual and skeleton (Thibault)
- CAD: B-Rep Euler Operators from QE (Tse)
- 3D kinetic Voronoi (Ledoux)
- 3D volumetric models (AQE) (Ledoux)
- Voronoi hierarchies
- AQE "Euler Operators" (Boguslawski)



## Building boundaries a) triangles b) Voronoi cells - built with kinetic DT/VD



## Compound Cells + Adjacency



## Euler Operators from QE



## **Building Extrusion from E-Os**



## Bridge or Hole from E-Os











#### Three-level Voronoi hierarchy





## **Full 3D Structures**

- The principles of planar graphs in 2D can be extended to volumetric graphs in 3D, with the addition of 3D volumes or "bubbles".
- Volumes are dual to nodes, and edges are dual to faces.
- We need to model solids, not just surfaces

#### Delaunay Tetrahedron/Voronoi Cell



## Extruded Buildings - just a surface model (B-Rep)



## True 3D Structures - dual links across the surface



# Full 3D Structures - interior volumes are included



# **3D Navigation**

- For many 3D urban applications we need to be able to navigate between rooms, etc.
- Our "Augmented Quad-Edge" structure makes this possible.
- Basically, it combines the surface model with the dual, penetrating edges.
- We can then navigate the graph between rooms, walls, etc.

## Navigation of Rooms and Walls - starting from qf we can find adjacent features



# **3D Object Reconstruction**

- We need to build our graph before we can use it.
- Individual pieces must be snapped together like "Lego".
- This is related to the "Euler Operators" used in CAD systems for surface models
- Using Half-AQE elements we can derive atomic construction elements

## Make Half-AQE



## **Connect Half-AQE**



## Make Face





## **Connect Neighbour Faces**



#### **Connect Adjacent Faces**



## Flip23 – Disconnect Cells



## Flip23 – Connect Cells



## Layer Model

Level 5: insertDelPoint

Level 4: flip14, flip23, flip32, makeOriginTetrahedron

- Level 3: connectFacesIntoTetrahedron, disconnectTetraIntoFaces
- Level 2: makeFace, connectAdjacentFaces, connectNeighbourFaces, disconnectNeighbourFaces
- Level 1: makeHalfAQE, connectHalfAQE, spliceHalfAQE, splice, changeVertex

Level 0: AQE

## **Properties and Conclusions**

- Associated HalfEdges in a primary and dual space are linked together permanently (Through pointer doesn't need to be changed)
- In a face approach, adjacent faces (from two adjacent cells) connected once are never disconnected. If there is need to remove face – two faces are removed simultaneously.
- It is possible to use an edge approach to build cells in our model. Both techniques can be mixed.
- We have a preliminary data structure for primal/dual navigation and construction